

# Natural control for multi-sided surfaces

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# Outline

## Motivation

## Generalized Bézier patches

- Curved domain

- Generalized B-spline patches

## Ribbon generation

- Cross-derivatives by parameters

## Interior control

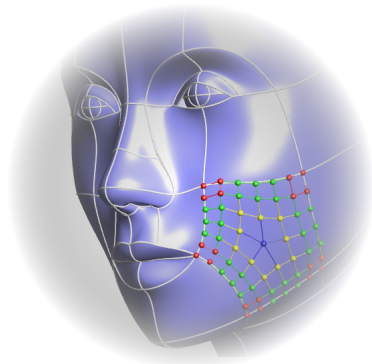
- Blending functions

## Tools for editing

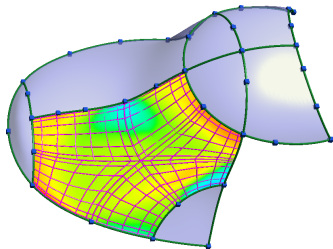
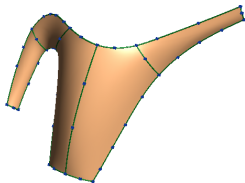
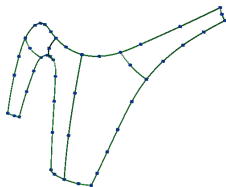
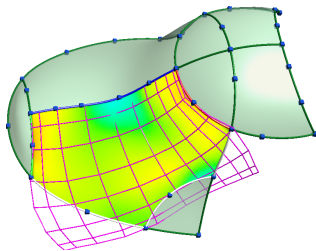
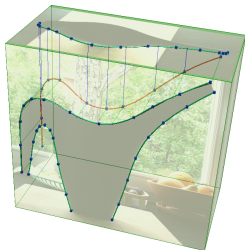
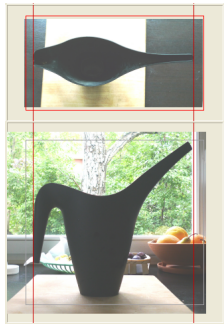
- Control vectors

- Proportional editing

## Conclusion



# Multi-sided surfaces





Contents lists available at [ScienceDirect](https://www.sciencedirect.com)

## Computer Aided Geometric Design

journal homepage: [www.elsevier.com/locate/cagd](https://www.elsevier.com/locate/cagd)



### Genuine multi-sided parametric surface patches – A survey

Tamás Várady, Péter Salvi\*, Márton Vaitkus

*Budapest University of Technology and Economics, Budapest, Hungary*

#### ARTICLE INFO

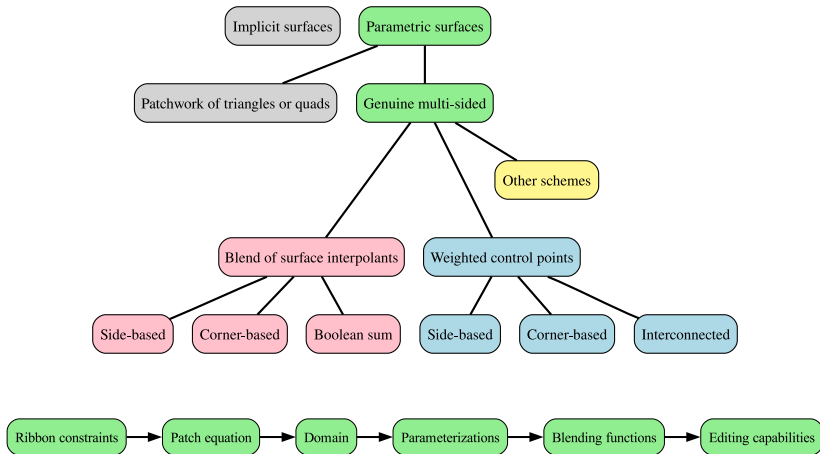
**Keywords:**

Multi-sided surfaces  
Ribbon-based surfaces  
Transfinite interpolation  
Control point patches  
Surface modeling  
General topology

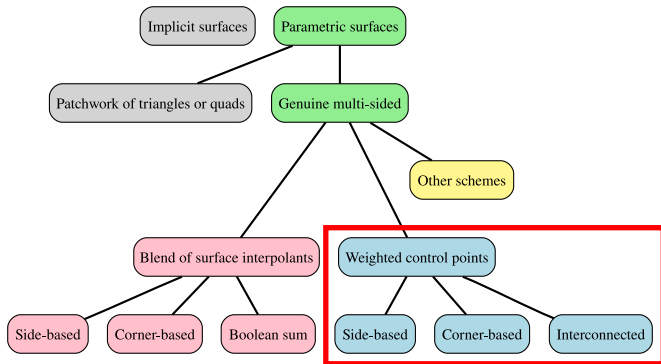
#### ABSTRACT

A state-of-the-art survey is presented on various formulations of multi-sided parametric surface patches, with a focus on methods that interpolate positional and cross-derivative information along boundaries.

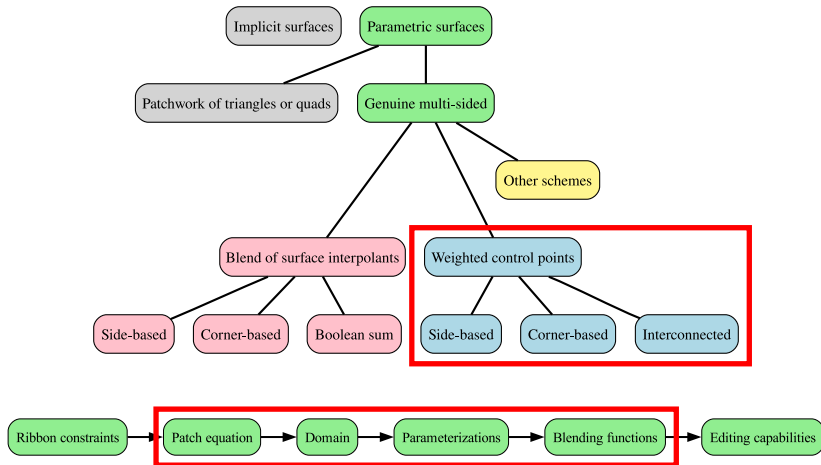
# Classification and constituents



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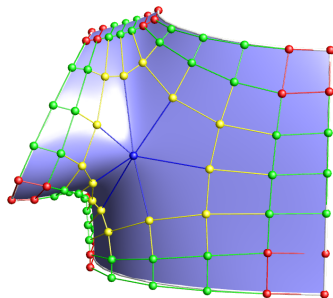
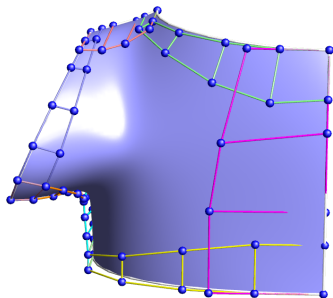
## Tools for editing

- Control vectors

- Proportional editing

## Conclusion

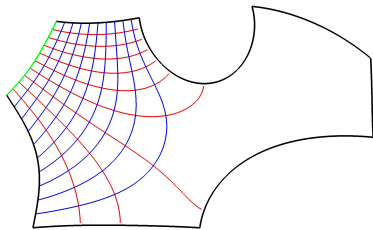
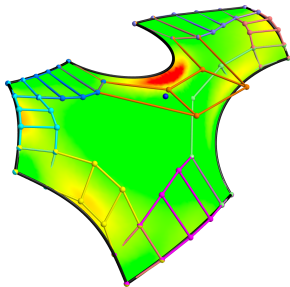
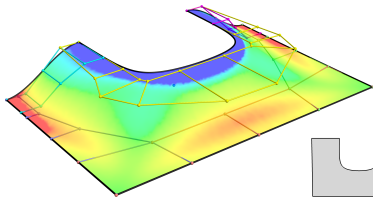
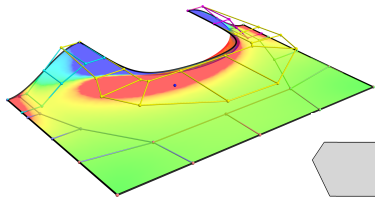
# Generalized Bézier patches



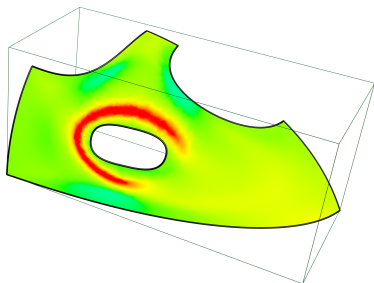
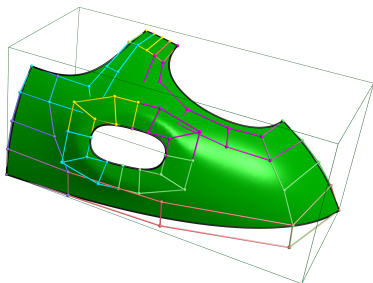
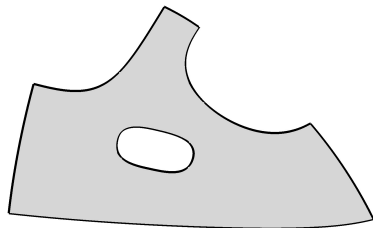
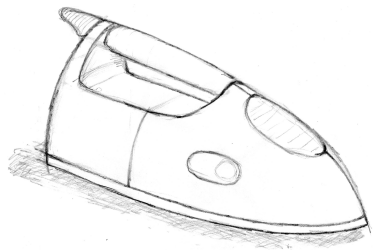
$$\mathbf{S}(u, v) = \sum_{i=1}^n \sum_{j=0}^d \sum_{k=0}^{(d-1) \div 2} \cdot \mathbf{C}_{ijk} \underline{\mu_{i,j,k}(u, v)} B_{i,j,k}^d(u, v) + \mathbf{C}_0 \cdot \underbrace{B_0(u, v)}_{1 - \sum \mu B}$$

$$B_{i,j,k}^d(u, v) := B_j^d(s_i(u, v)) \cdot B_k^d(h_i(u, v)) \text{ with } (s_i, h_i) \text{ local parameters}$$

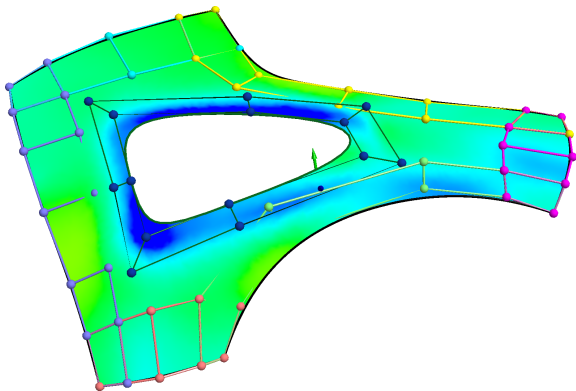
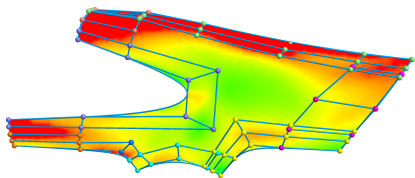
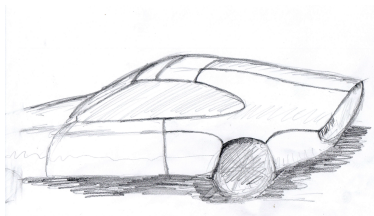
## Curved domain



## Multi-connected domains



# Generalized B-spline patches



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Generalized B-spline patches

Ribbon generation

Cross-derivatives by parameters

Interior control

Blending functions

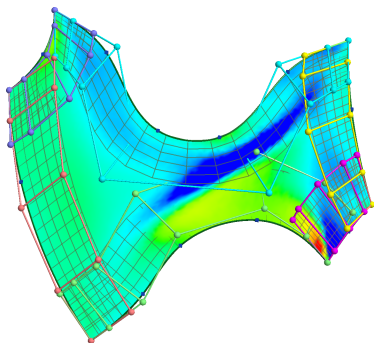
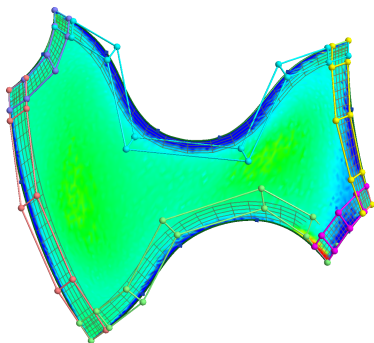
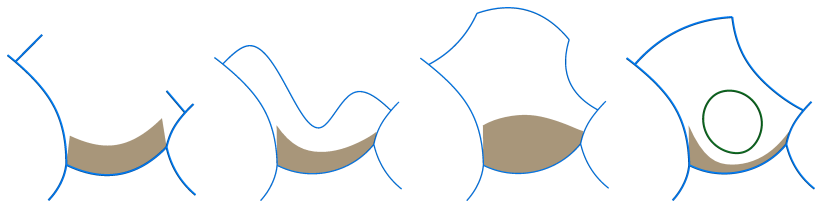
Tools for editing

Control vectors

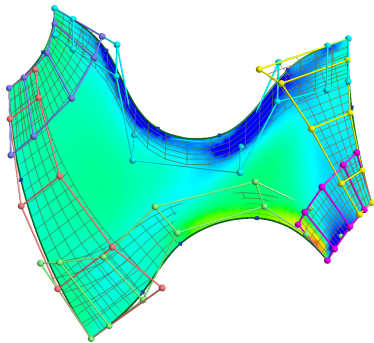
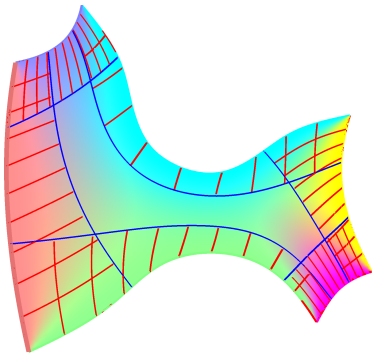
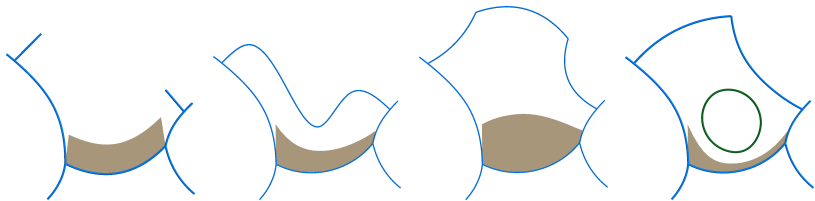
Proportional editing

Conclusion

## Cross-derivative strength



## Setting by local parameters



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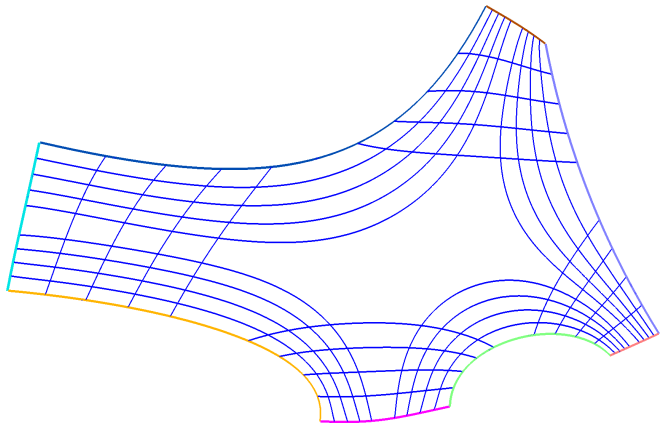
Tools for editing

Control vectors

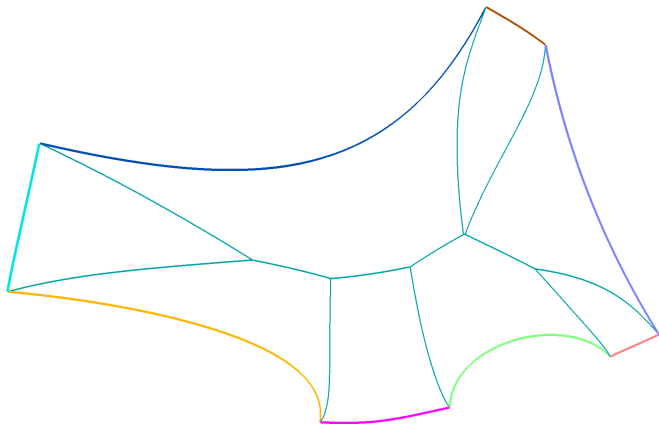
Proportional editing

Conclusion

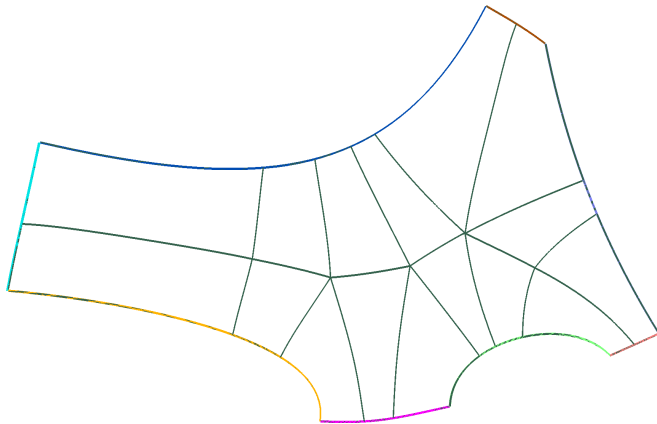
## 'Templates' from medial axis – distance parameters



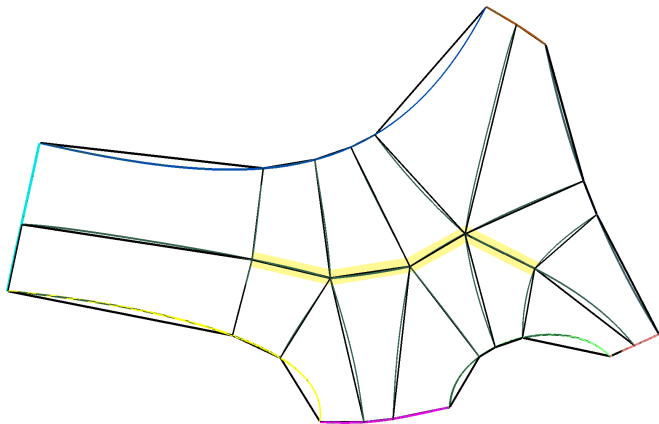
## 'Templates' from medial axis – parametric medial axis



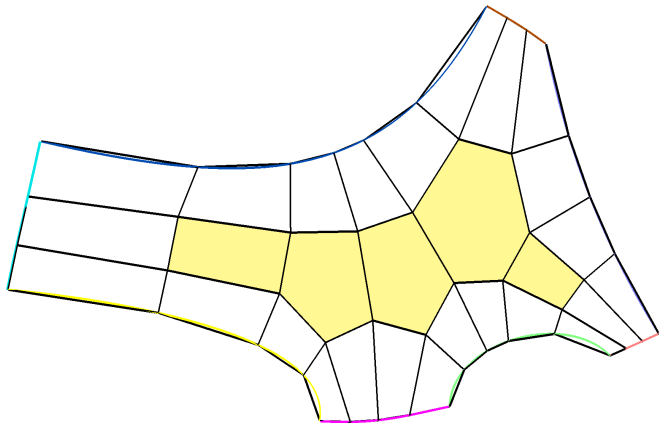
## 'Templates' from medial axis – MAT-based quad structure



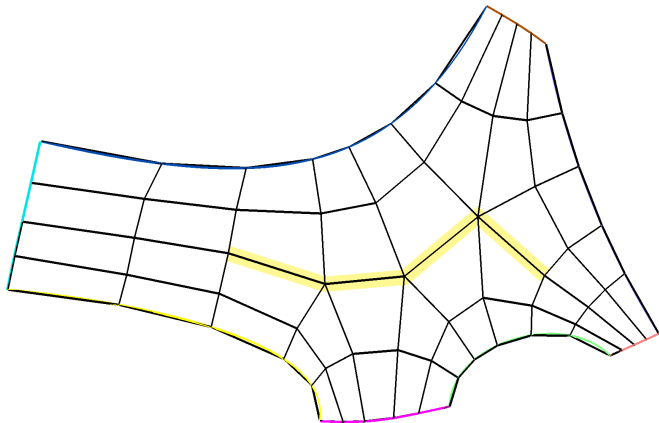
## 'Templates' from medial axis – $T_2$ skeleton



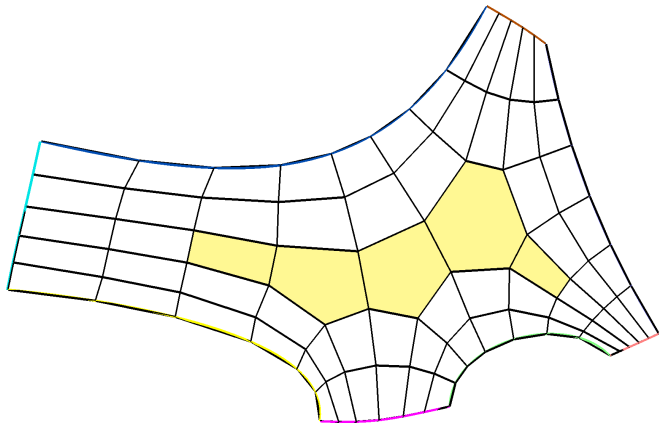
## 'Templates' from medial axis – $T3$ skeleton



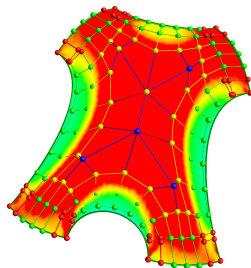
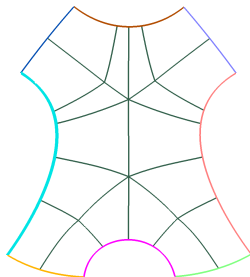
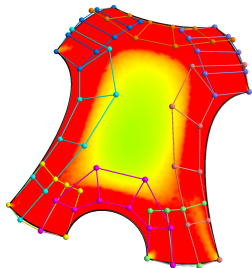
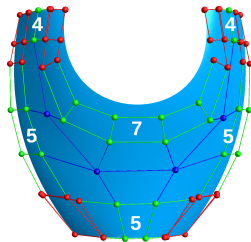
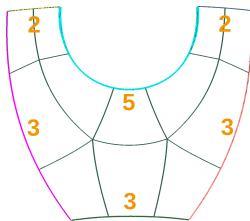
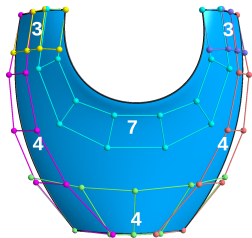
## 'Templates' from medial axis – $T_4$ skeleton



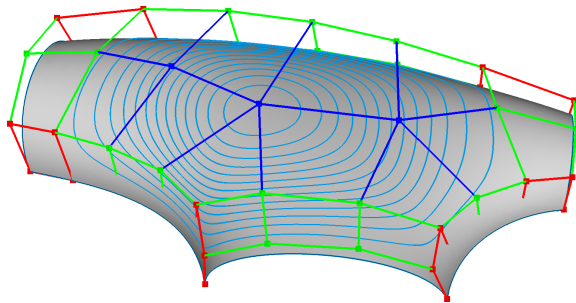
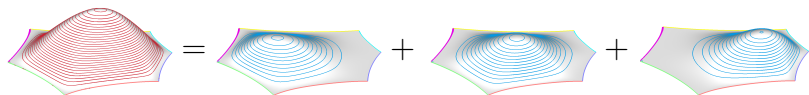
## 'Templates' from medial axis – *T5* skeleton



# Degree synchronization



# Distributing weight deficiency proportionally



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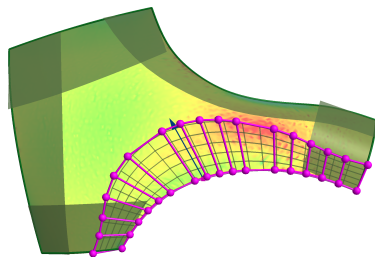
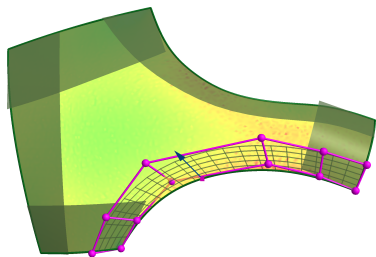
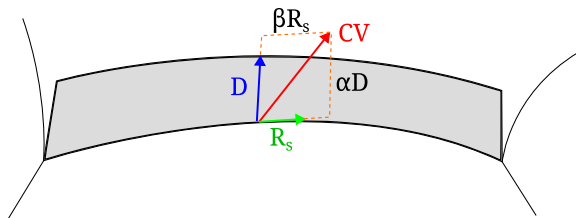
## Tools for editing

- Control vectors

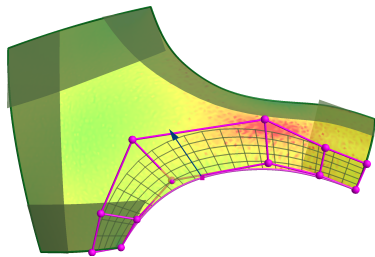
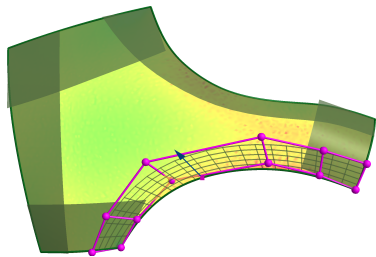
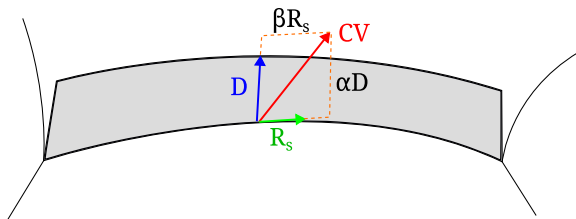
- Proportional editing

## Conclusion

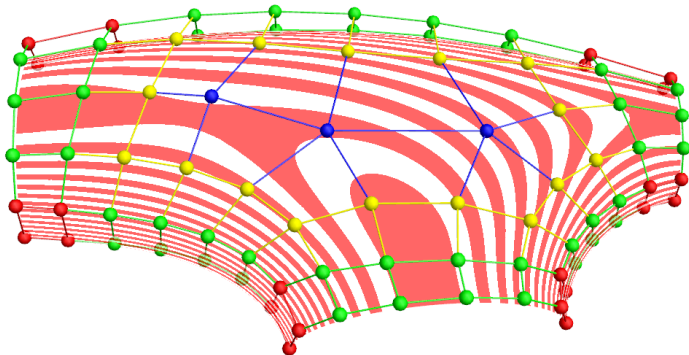
# Editing boundaries by control vectors – Exact $G^1$



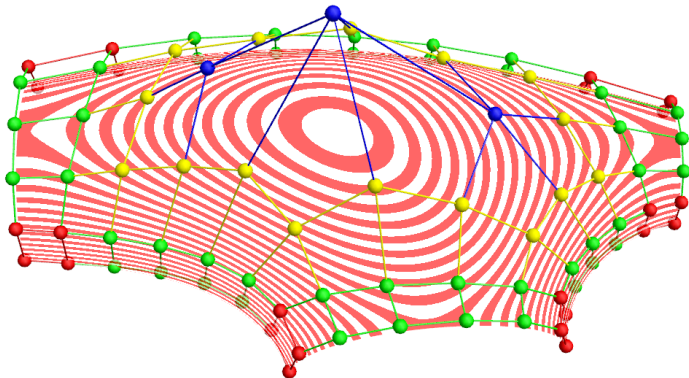
# Editing boundaries by control vectors – Approximate $G^1$



## Editing the interior proportionally



## Editing the interior proportionally



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## Conclusion & future work

- ▶ Curved, multi-connected domains
  - ▶ Handling of highly curved boundaries
  - ▶ Natural cross-derivative lengths
  - ▶ MAT  $\rightarrow$  interior control structure
- ▶ Interior blends
  - ▶ Proportional weight deficiency distribution
- ▶ Editing
  - ▶ Boundary CPs  $\rightarrow$  implicitly by control vectors
  - ▶ Interior CPs  $\rightarrow$  simultaneously with a falloff function



Next: interior control structure for generalized B-spline surfaces

## Related papers

### 1. Multi-sided patch survey

T. Várady, P. Salvi, M. Vaitkus:

*Genuine multi-sided parametric surface patches – a survey.*

**Computer Aided Geometric Design**, Vol. 110, #102286, 2024.

### 2. Modeling with control vectors

P. Salvi, M. Vaitkus, T. Várady:

*Constrained modeling of multi-sided patches.*

**Computers and Graphics**, Vol. 114, pp. 86–95, 2023.

### 3. Independent interior controls

P. Salvi:

*Intuitive interior control for multi-sided patches with arbitrary boundaries.*

**Computer-Aided Design and Applications**, Vol. 21(1), pp. 143–154, 2024.

### 4. MAT-based interior controls

M. Vaitkus, P. Salvi, T. Várady:

*Interior control structure for Generalized Bézier patches over curved domains.*

**Computers and Graphics**, 2024. (accepted for SMI'24)



<https://3dgeo.iit.bme.hu/>